

# Inductors

$$V_L = L \frac{dI}{dt}$$

equation



symbol

$$L = [H] = [\text{henry}]$$

$$[H] = \left[ \frac{\text{kg m}^2}{\text{amp}^2 \text{s}^2} \right]$$

units

if  $I(t) = I_p \sin(\omega t - \phi_i)$

then:  $V_L = L \frac{d}{dt} (I_p \sin(\omega t - \phi_i))$

$$= \omega L I_p \cos(\omega t - \phi_i)$$

$$V_L = \omega L I_p \sin(\omega t - \phi_i + \frac{\pi}{2})$$

in time domain  $V_L$  lags the current by  $90^\circ$

move to complex plane:

$$V_L = \text{Im} ( \omega L I_p e^{i(\omega t - \phi_i + \frac{\pi}{2})} )$$

$$= \text{Im} ( \omega L I_p e^{i\omega t} e^{-i\phi_i} e^{i\frac{\pi}{2}} )$$

$$= \text{Im} ( i\omega L I_p e^{-i\phi_i} e^{i\omega t} )$$

move to phasor reference frame:

$$\text{Im} (\tilde{V}_L e^{i\omega t}) = \text{Im} (i\omega L \tilde{I} e^{i\omega t})$$

↑ rotating reference frame

where:  $\tilde{V}_L = V_{L,p} e^{-i\phi_V}$  &  $\tilde{I} = I_p e^{-i\phi_i}$

separate phasor part:

$$\tilde{V}_L = i\omega L \tilde{I}$$

$$\tilde{V}_L = Z_L \tilde{I}$$

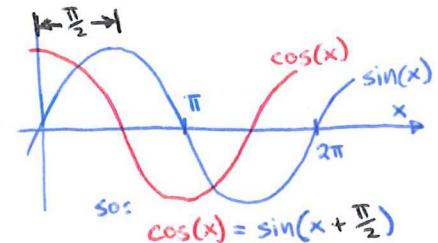
in phase domain

where

$$Z_L = i\omega L$$

$Z_L$  is Imaginary and is  $+90^\circ$  to the real axis

$$\cos(x) = \sin(x + \frac{\pi}{2})$$

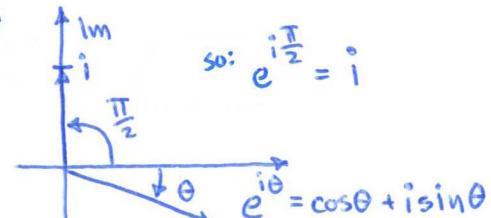


$$e^{i\theta} = \cos\theta + i\sin\theta$$

$$x^{m+n} = x^m x^n$$

$$e^{i\frac{\pi}{2}} = i$$

phasors



$$\text{so: } e^{i\frac{\pi}{2}} = i$$

$$\begin{aligned} \text{so: } & \text{Re}(e^{i\theta}) = \cos\theta \\ & \text{Im}(e^{i\theta}) = \sin\theta \end{aligned}$$

Phasors:

